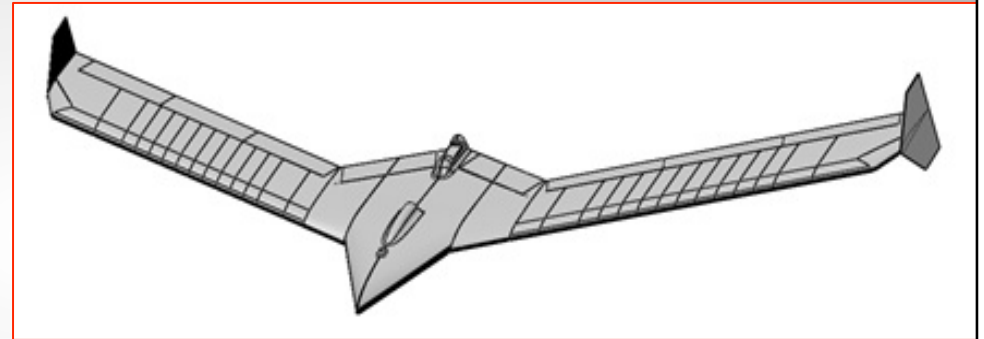


# **Flight-Dynamics, Flutter, and Active-Flutter-Suppression Analyses of a Flexible Flying-Wing Research Drone**

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**Principal**  
**D.K. Schmidt, & Associates**



**As presented at the**

**NASA Armstrong Flight Research Center**  
**Edwards AFB, CA**

**June 15, 2015**

# **The Overall Research Project**

## **Lightweight Adaptive Aeroelastic Wing**

Funded Under the  
**NASA AATT Program**

### **The Team**

**University of Minnesota**  
**Pete Seiler (Gary Balas)**

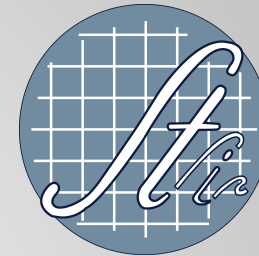
**Systems Technology Inc.**  
**Brian Danowsky**

**VPI&SU - Rakesh Kapania**

**Aurora Flight Sciences**  
**Jeremy Hollman**

**CM Soft Inc. – Charbel Farhat**

**D.K. Schmidt & Associates**



# Project Overview

Goal: Actively Optimize Wing Shape - Transport Aircraft

Approach: Use Flexibility to an Advantage, MDAO, active control

- Active flutter suppression is a key enabling technology
- Critical PAAW program components –

Three different vehicles will be developed and flight tested

The first will be very similar to Lockheed Martin's FFAD  
- which is the vehicle being discussed here

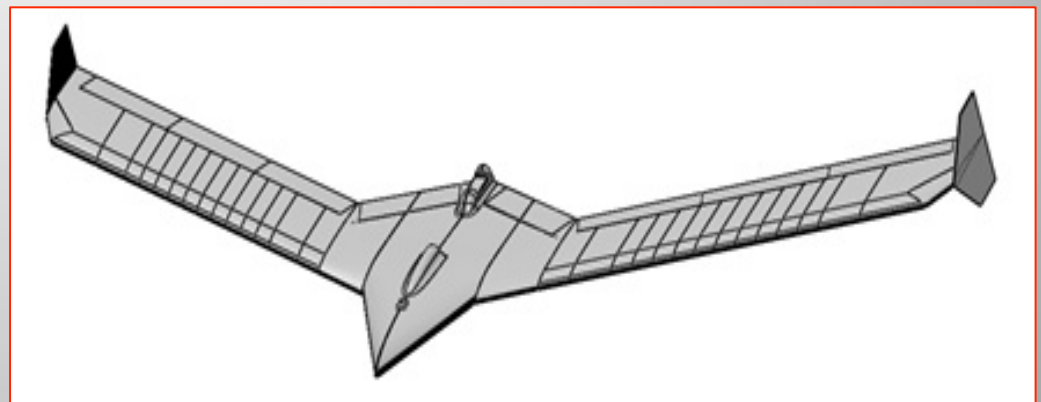
Weight

12 lb

Wing Span

10 ft

“Rigid” center body – flex wings



# Outline

- Objectives and motivation
- The modeling methodology
- The vehicle's attitude dynamics  
Rigid and Elastic
- Flutter analysis
- Active flutter suppression
- Summary and conclusions

# Objectives of this Investigation

- Assess the flutter and flight-dynamics characteristics of FFAD vehicle
- Synthesize integrated SAS/Active Flutter Suppression CLAWS (with no a priori knowledge of LM's CLAWS)
- Develop dynamic nDOF model early in design cycle
- Although several modeling approaches will be utilized in project, this task was is to-

Explore the use of a “Flight-Dynamics” model, as opposed to a more traditional “Flutter” model

Consider use of beam-element FEM and quasi-steady aero initially

- Feedback and suggestions sought
- NOTE: Longitudinal axis only, so far

# **“Flutter” vs. “Flight-Dynamics” nDOF Models**

## **Flutter Based**

**Expand flutter model  
(elastic DOFs) to  
incorporate RB DOFs**

**EOMs in inertial frame**

**Linear**

**Familiar to aeroelasticians**

## **Flight-Dynamics Based**

**Expand flight-dynamics  
model (RB DOFs) to  
incorporate elastic DOFs**

**EOMs in vehicle-fixed frame**

**Linear (with potential for  
non-linear RB EOMs)**

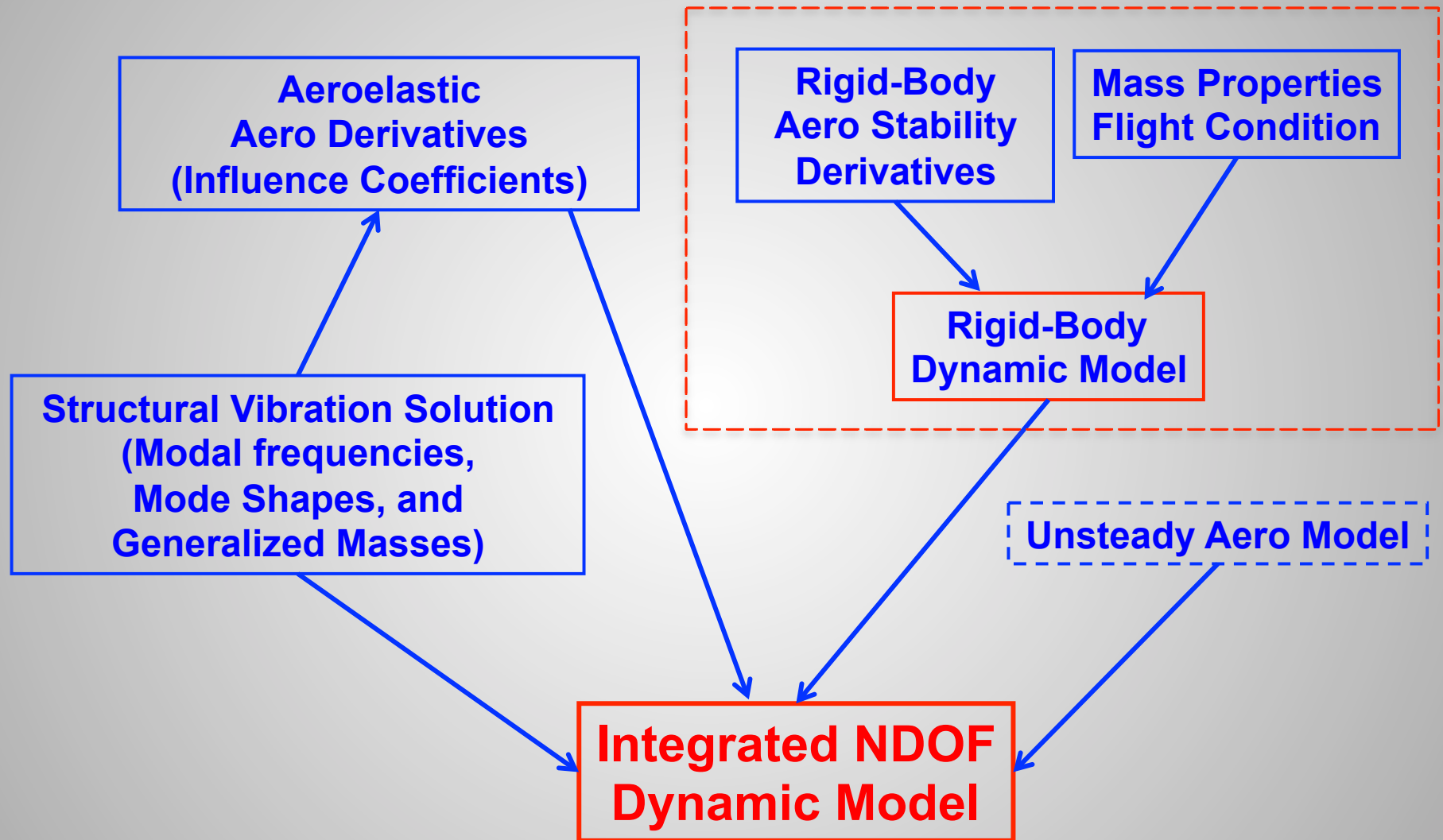
**Familiar to flight dynamicists**

# The “Flight-Dynamics” Modeling Formulation

- Based on mean-axis formulation of Milne (1964)\*
- Mean axes replace the body-fixed axes used for rigid vehicles, as their motion describes the RB motion (DOFs), structure deforms relative to this mean axis
- EOMs expressed in “body-fixed” vs inertial axes and expressed in terms of aero coefficients - typical of flight-dynamics models of rigid vehicles.
- EOMs derived via Lagrange using method of assumed modes
- Uses free-free vibration mode shapes (NASTRAN) for the shape functions, thus satisfying Milne’s mean-axis constraints
- Various aerodynamic modeling approaches – wind tunnel, slender-wing, VLM, DLM

- Milne, “Dynamics of the Deformable Airplane,” UK Ministry of Aviation, Aero Res Council Rept. 1964.
- Waszak and Schmidt, “Flight Dynamics of Aeroelastic Vehicles,” *Journ. of AC*, 25 (6), June, 1988.
- Schmidt, *Modern Flight Dynamics*, McGraw Hill, 2012.

# The Modeling Methodology





# NDOF Model Structure

## Longitudinal Dynamics

$$\mathbf{x}^T = \left[ \begin{array}{cccc|cccccc} u_{rig} & \alpha_{rig} & \theta_{rig} & q_{rig} & \eta_1 & \dot{\eta}_1 & \eta_2 & \dot{\eta}_2 & \eta_3 & \dot{\eta}_3 \end{array} \right]$$

$$\mathbf{A} = \left[ \begin{array}{cccc|cccccc} X_u & X_\alpha & -g & X_q & 0 & 0 & \dots & 0 & 0 \\ Z_u/U_0 & Z_\alpha/U_0 & 0 & 1+Z_q/U_0 & Z_{\eta_1}/U_0 & Z_{\dot{\eta}_1}/U_0 & \dots & Z_{\eta_3}/U_0 & Z_{\dot{\eta}_3}/U_0 \\ 0 & 0 & 0 & 1 & 0 & 0 & \dots & 0 & 0 \\ M_u & M_\alpha & 0 & M_q & M_{\eta_1} & M_{\dot{\eta}_1} & \dots & M_{\eta_3} & M_{\dot{\eta}_3} \\ \hline 0 & 0 & 0 & 0 & 0 & 1 & \dots & 0 & 0 \\ 0 & \Xi_{1_\alpha} & 0 & \Xi_{1_q} & \Xi_{1_{\eta_1}} - \omega_1^2 & \Xi_{1_{\dot{\eta}_1}} - 2\zeta_1\omega_1 & \dots & \Xi_{1_{\eta_3}} & \Xi_{1_{\dot{\eta}_3}} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \dots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & \dots & 0 & 1 \\ 0 & \Xi_{3_\alpha} & 0 & \Xi_{3_q} & \Xi_{0_{\eta_1}} & \Xi_{3_{\dot{\eta}_1}} & \dots & \Xi_{3_{\eta_3}} - \omega_3^2 & \Xi_{3_{\dot{\eta}_3}} - 2\zeta_3\omega_3 \end{array} \right]$$

$$\mathbf{A} = \left[ \begin{array}{cc|cc} \mathbf{A}_{RR} & & \mathbf{A}_{RE} & \\ \hline \mathbf{A}_{ER} & & \mathbf{A}_{EE} & \end{array} \right]$$

# Rigid-Body Longitudinal Attitude Dynamics

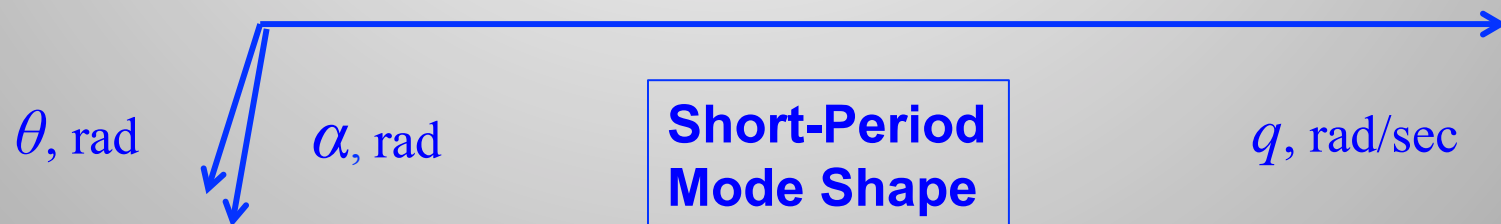
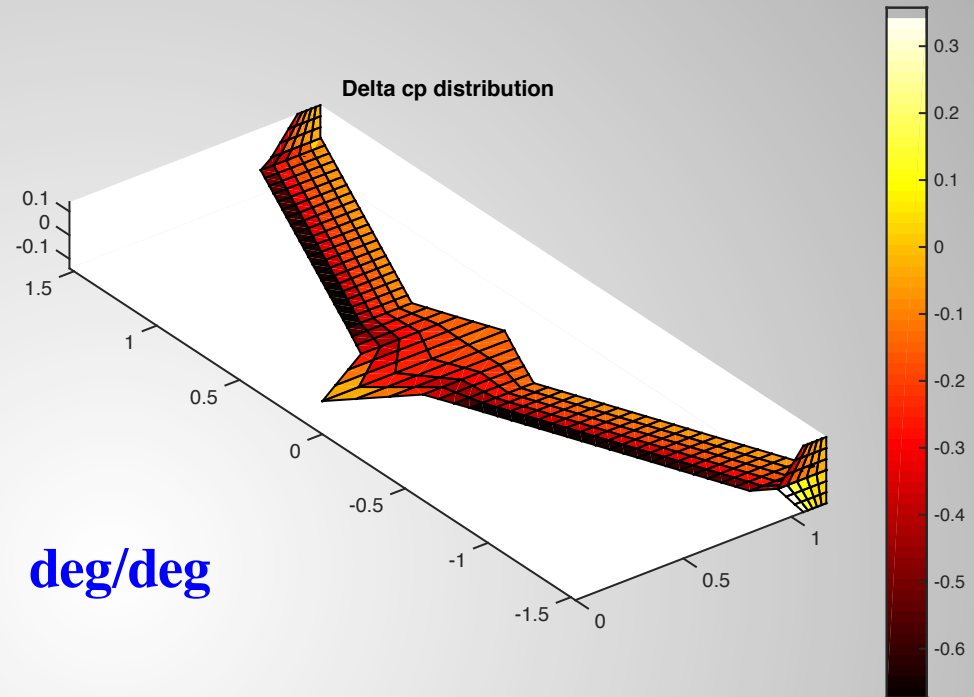
35 kt

SM = 6%

Conventional modes

$$\frac{\theta(s)}{-\delta_E(s)} = \frac{105.0 [0.049][6.66]}{[-0.01, 0.54][0.73, 12.4]} \quad \text{deg/deg}$$

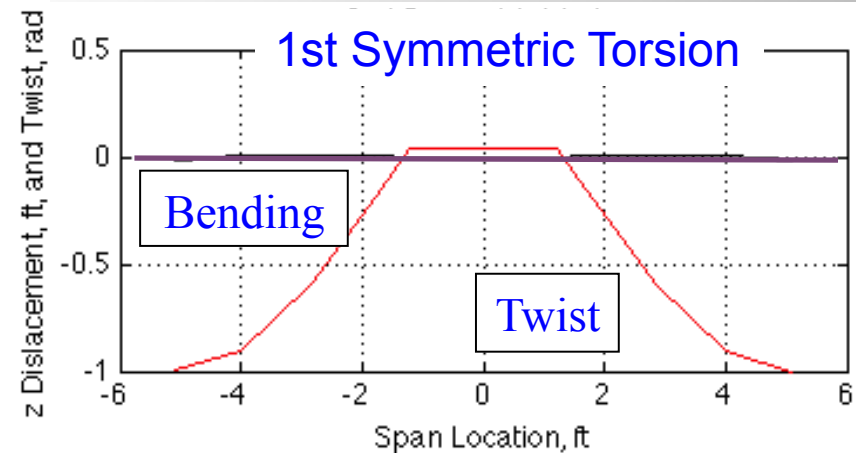
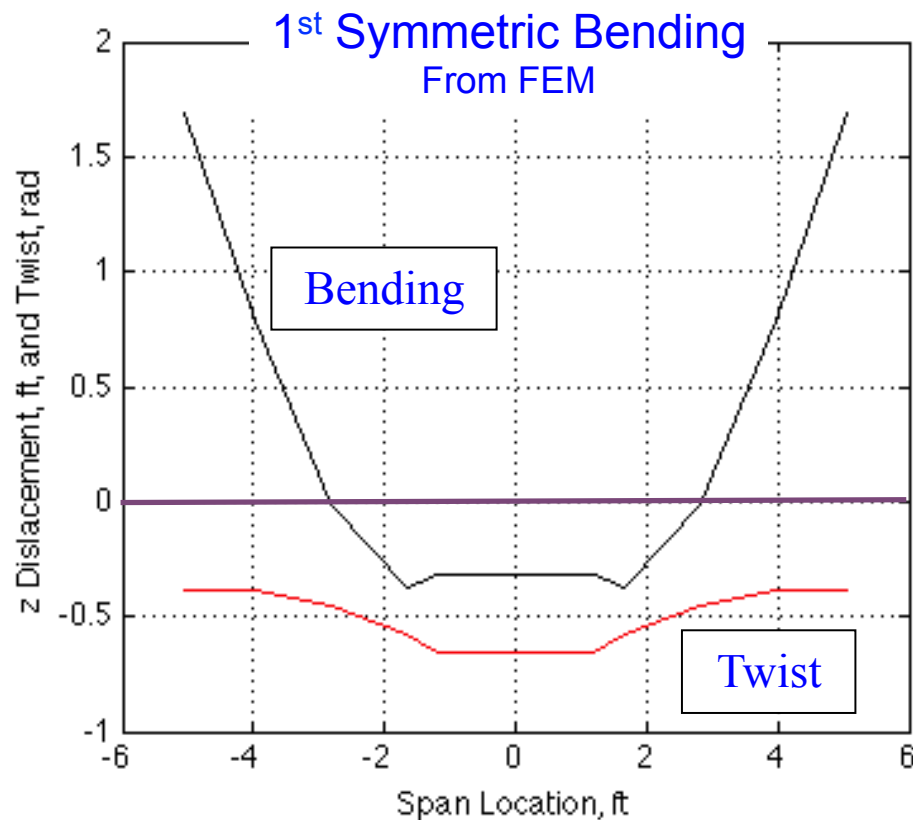
$$\frac{n_{Zcg}(s)}{-\delta_E(s)} = \frac{3.38 [0][-0.285][0.362][5.64]}{[-0.01, 0.54][0.73, 12.4]} \quad \text{g/deg}$$



# Structural Dynamics

## Symmetric Free-Free Vibration Modes

Data and Source	Sym 1 <sup>st</sup> Bending	Sym 1 <sup>st</sup> Torsion	Sym 2 <sup>nd</sup> Bending
Frequency, UMN (GVT)	34.6 r/s	117.8 r/s	145.6 r/s
Frequency, LM	35.4 r/s	123.4 r/s	147.3 r/s
Damping, UMN (GVT)	1.55%	2.06%	2.85%
Gen. Mass, UMN (FEM)	0.28950 sl-ft <sup>2</sup>	0.00772 sl-ft <sup>2</sup>	0.05239 sl-ft <sup>2</sup>



**Knowing The Mode Shapes  
Is Critical**

# Elastic Vehicle Attitude Dynamics

$$35 \text{ kt} < V_{F1}$$

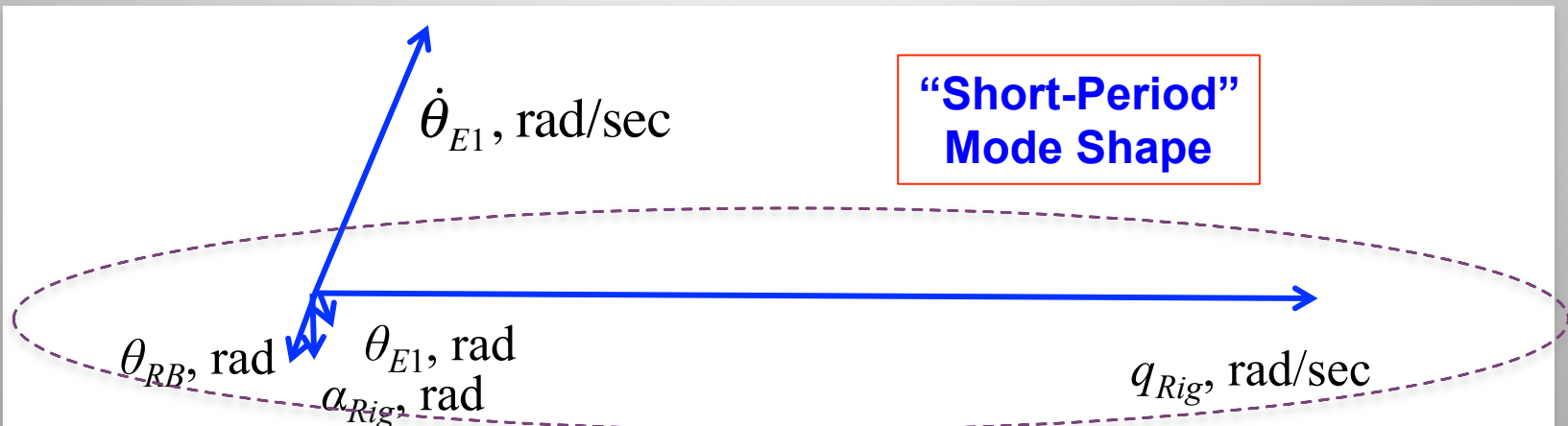
$$\frac{\theta_{cg}(s)}{-\delta_E(s)} = \frac{65.2 \begin{bmatrix} 0.0536 \end{bmatrix} \begin{bmatrix} 7.044 \end{bmatrix} \begin{bmatrix} 0.22, 41.2 \end{bmatrix} \begin{bmatrix} 0.05, 101.7 \end{bmatrix} \begin{bmatrix} 0.05, 165.3 \end{bmatrix}}{\begin{bmatrix} -0.01, 0.61 \end{bmatrix} \begin{bmatrix} 0.59, 18.1 \end{bmatrix} \begin{bmatrix} 0.15, 30.9 \end{bmatrix} \begin{bmatrix} 0.07, 103.7 \end{bmatrix} \begin{bmatrix} 0.08, 146.0 \end{bmatrix}} \text{ deg/deg}$$

$$\frac{n_{Zcg}(s)}{-\delta_E(s)} = \frac{-0.228 \begin{bmatrix} 0 \end{bmatrix} \begin{bmatrix} -0.0279 \end{bmatrix} \begin{bmatrix} 29.58 \end{bmatrix} \begin{bmatrix} -25.58 \end{bmatrix} \begin{bmatrix} 0.24, 42.3 \end{bmatrix} \begin{bmatrix} 0.07, 104.1 \end{bmatrix} \begin{bmatrix} -282.6 \end{bmatrix} \begin{bmatrix} 246 \end{bmatrix}}{\begin{bmatrix} -0.01, 0.61 \end{bmatrix} \begin{bmatrix} 0.59, 18.1 \end{bmatrix} \begin{bmatrix} 0.15, 30.9 \end{bmatrix} \begin{bmatrix} 0.07, 103.7 \end{bmatrix} \begin{bmatrix} 0.08, 146.0 \end{bmatrix}} \text{ g/deg}$$

Rigid

$$\frac{\theta(s)}{-\delta_E(s)} = \frac{105.0 \begin{bmatrix} 0.049 \end{bmatrix} \begin{bmatrix} 6.66 \end{bmatrix}}{\begin{bmatrix} -0.01, 0.54 \end{bmatrix} \begin{bmatrix} 0.73, 12.4 \end{bmatrix}} \text{ deg/deg}$$

$$\frac{n_{Zcg}(s)}{-\delta_E(s)} = \frac{3.38 \begin{bmatrix} 0 \end{bmatrix} \begin{bmatrix} -0.285 \end{bmatrix} \begin{bmatrix} 0.362 \end{bmatrix} \begin{bmatrix} 5.64 \end{bmatrix}}{\begin{bmatrix} -0.01, 0.54 \end{bmatrix} \begin{bmatrix} 0.73, 12.4 \end{bmatrix}} \text{ g/deg}$$



# Elastic Vehicle Attitude Dynamics

$$35 \text{ kt} < V_{F1}$$

No classical short-period mode  
“Elastic-short-period mode”

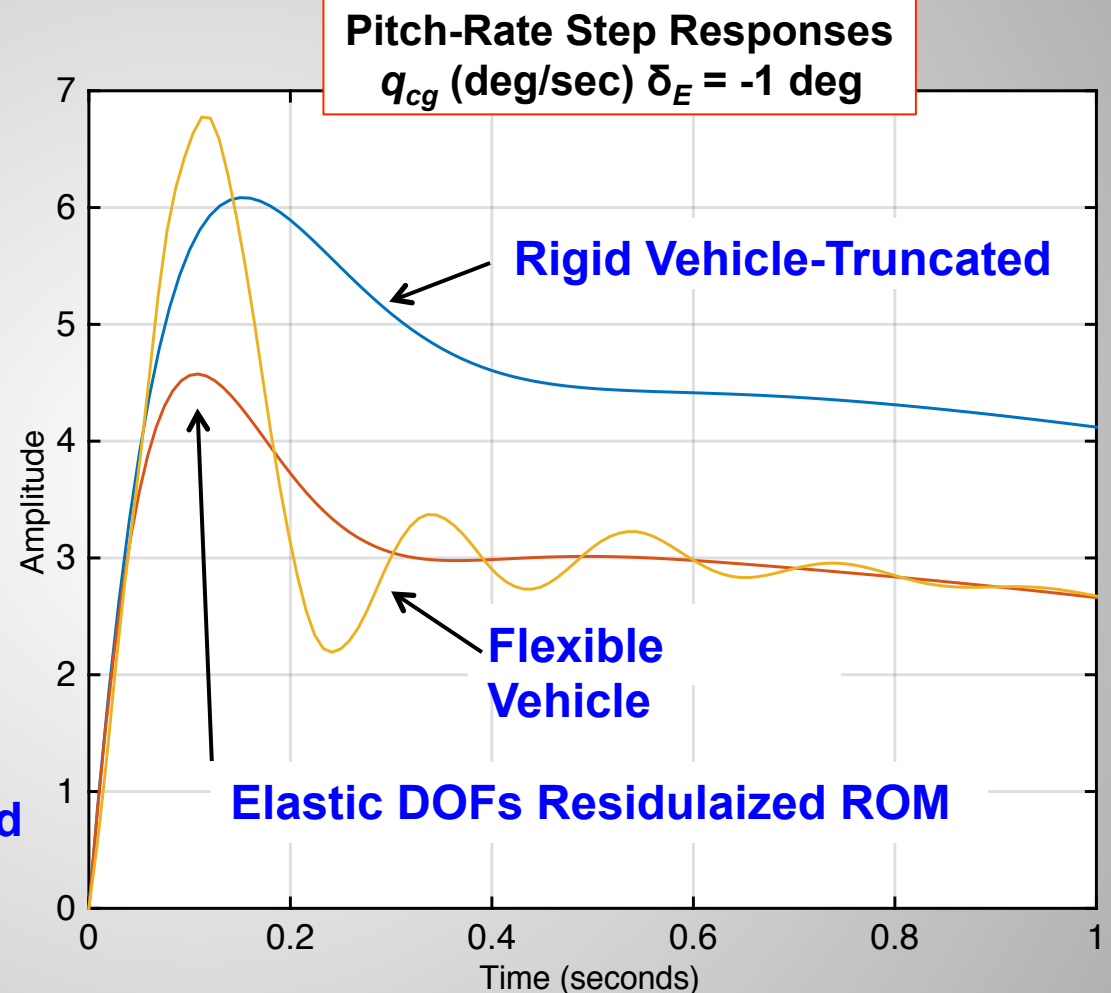
Pitch attitude highly coupled  
with aeroelastic response  
(1<sup>st</sup> bending/tors. vibr. mode)

“Short Period” –  
Higher frequency,  
lower damping

$1/T_{\theta 2}$  Increased

$n_z$  Numerator dynamics affected

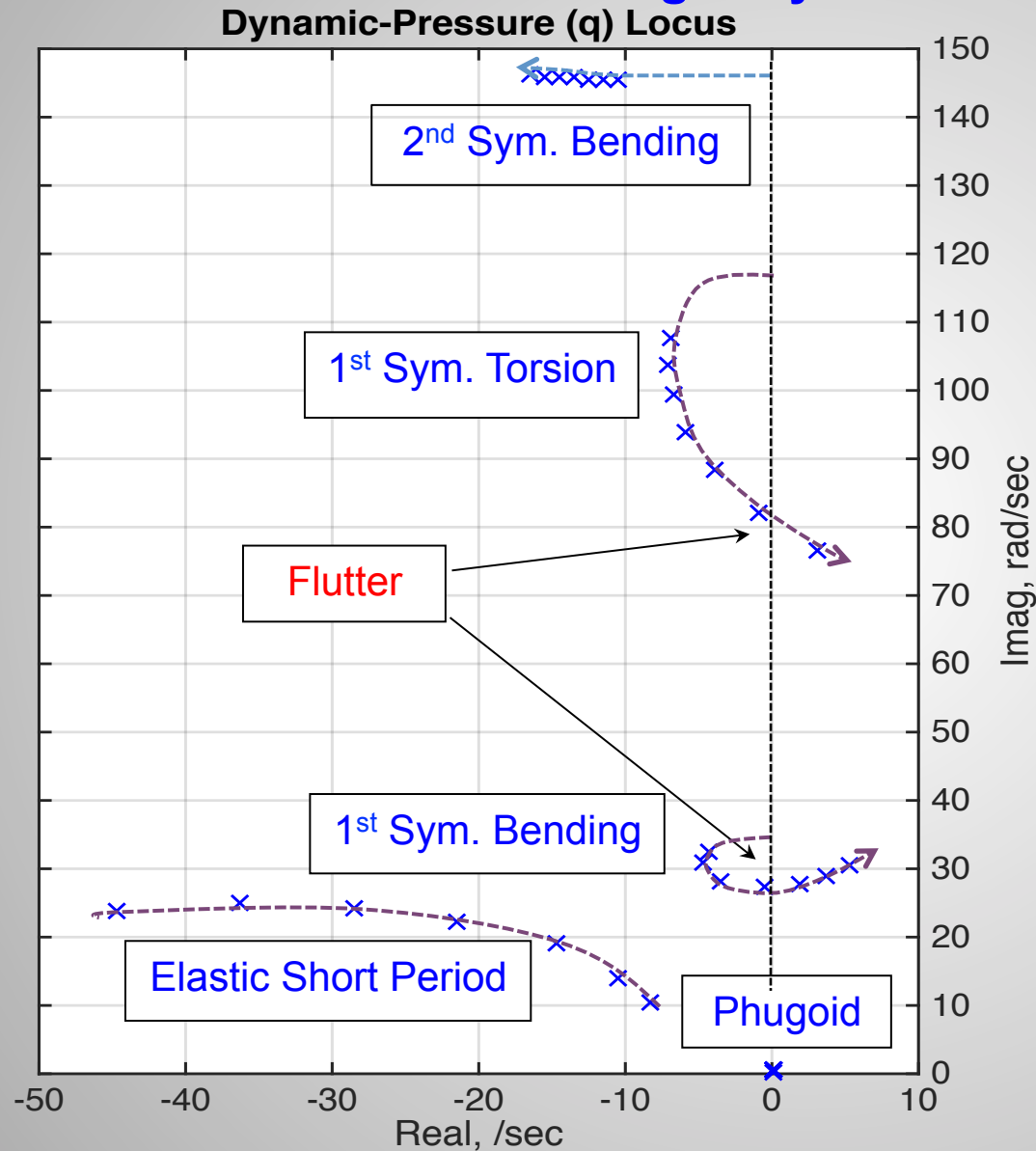
Higher-order elastic dipoles



# **Flutter Analysis**

# Flutter Analysis - q Locus

From “Flight Dynamics” Model



BFF Vehicle  
Longitudinal Dynamics  
Sea Level

Two flutter conditions

BFF and BT flutter

BFF  $V_{\text{flutter}} = 47$  kt.

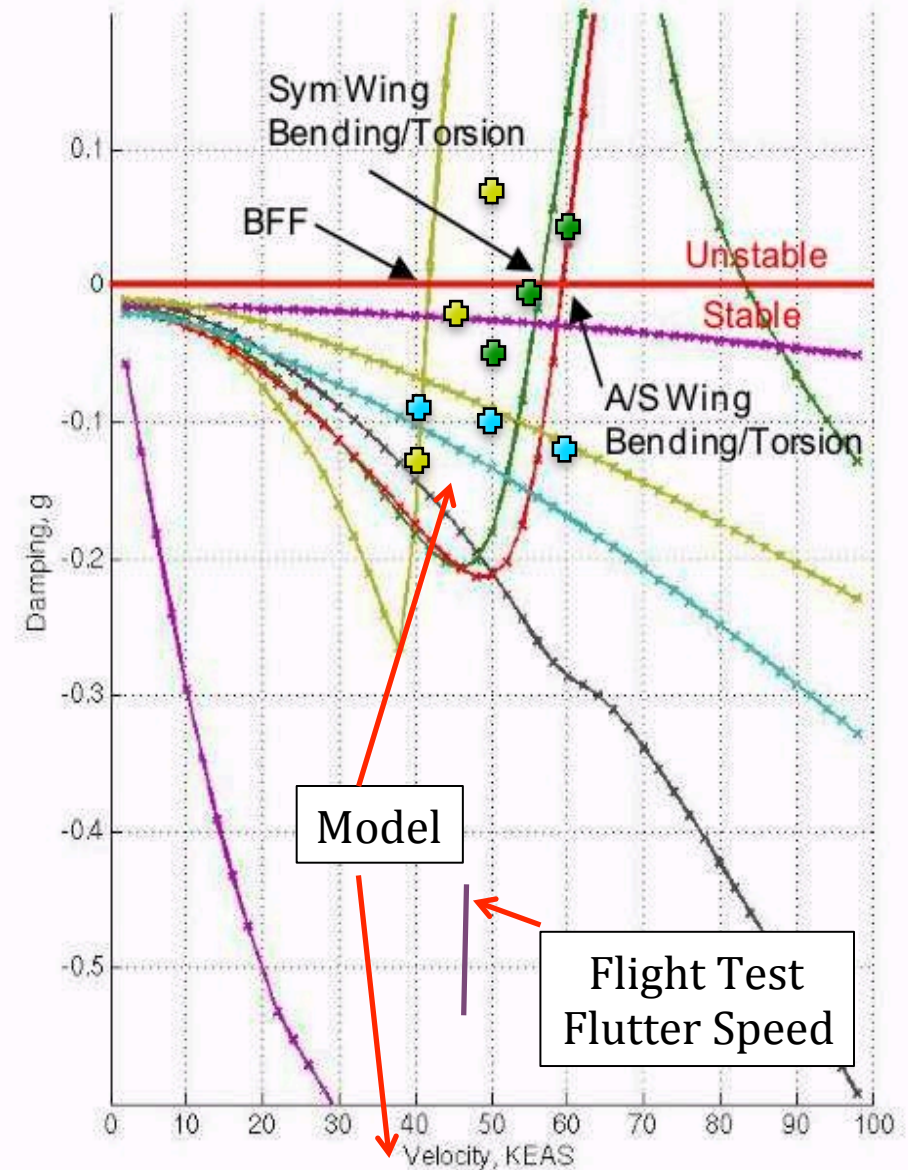
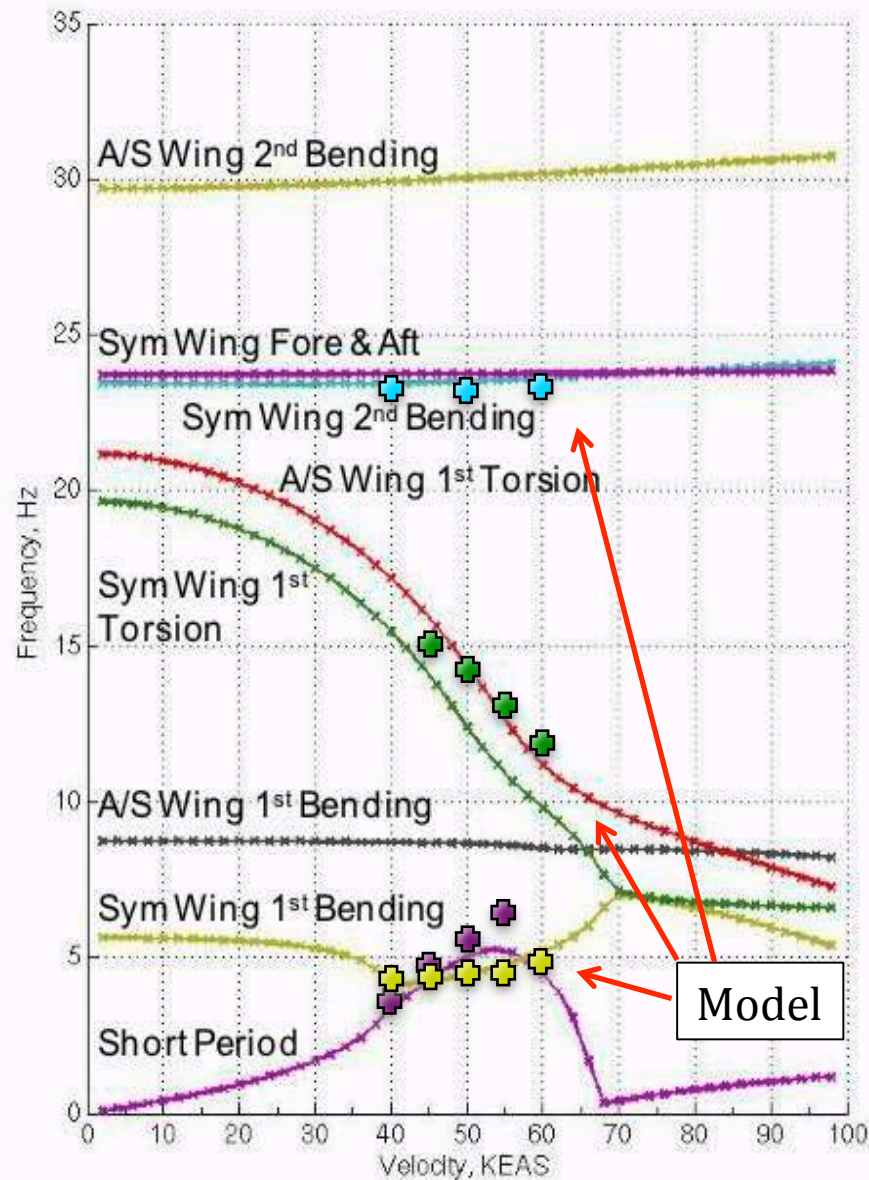
BT  $V_{\text{flutter}} = 57$  kt.

BFF genesis mode –  
1<sup>st</sup> symmetric bending

BT genesis mode –  
1<sup>st</sup> symmetric torsion



# VFG Comparison





# Comparison With LM Results\*

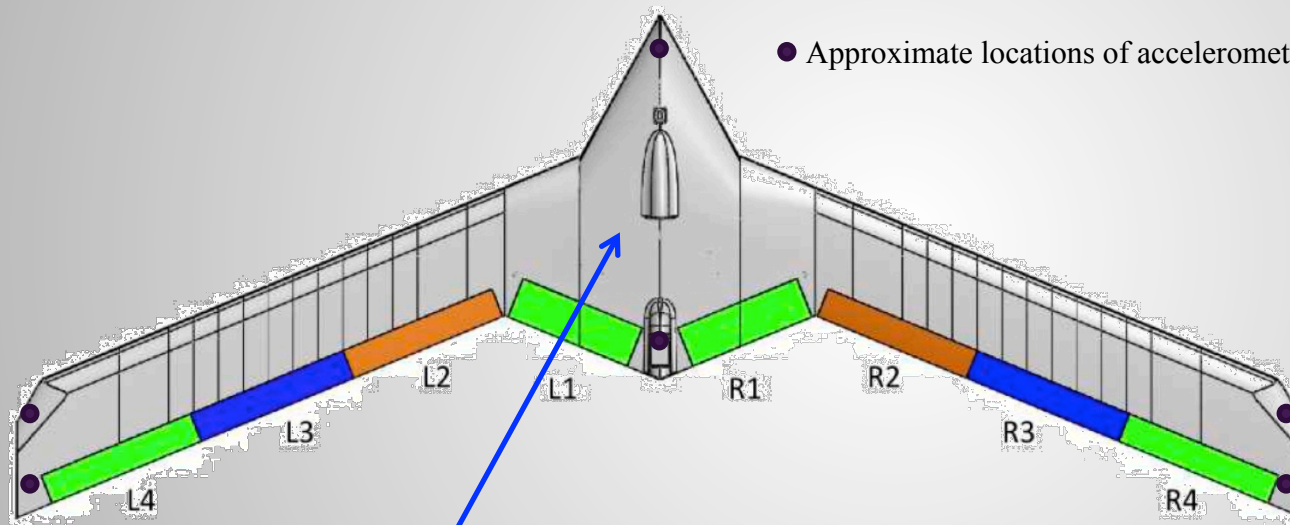
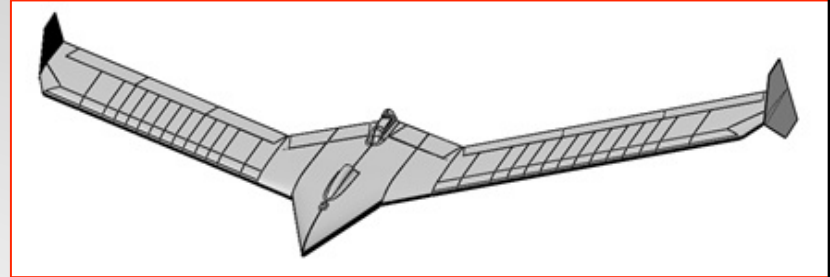
Model/Test	BFF Flutter Speed	BFF Flutter Frequency	BT Flutter Speed	BT Flutter Frequency
LM Analytical	43 kt	4.2 Hz	57 kt	10.5 Hz
LM Flight Test	46 kt	4.5 Hz	NA	NA
FD Model	47 kt	4.4 Hz	57 kt#	12.7 Hz
Residualized FD Model	47 kt	4.4 HZ	NA	NA
Truncated FD Model	No Flutter	No Flutter	NA	NA

- **Correctly captured both flutter modes**
- **Matched both genesis flutter modes**
- **Matched BFF flutter speed - # BT Adjusted**
- **Matched BFF Flutter frequency**
- **Torsion mode SE aero effects critical to BFF condition**

• Burnett, Edward L., et al, "NDOF Simulation Model for Flight Control Development with Flight Test Correlation," Lockheed Martin Aeronautics Co., AIAA Modeling and Simulation Tech. Conf., 2010-7780, 2010.

# **Active Flutter Suppression and Stability Augmentation**

# Vehicle Sensors and Control Surfaces



● Approximate locations of accelerometers

FCS

Gyros. Accels, GPS

Body Flaps	L1 – R1
Aileron	L2 – R2
Elevator	L3 – R3
OB Flaps	L4 – R4

# Control-Law Synthesis - ILAF

- Require integrated approach to SAS and active flutter suppression
- Seek robustness against vibration mode-shape uncertainty
- One approach - concept of ILAF (Wykes\*)  
“Identically Located Acceleration and Force”

- ILAF – “A point force applied to a structure proportional to the velocity of the structure measured at the point of application of the force will increase the damping of all structural modes.”
  - Requires no knowledge of the vibration mode shapes – robust  
If can implement true ILAF – point force.
- Used to design active-structural-mode-control system on B-1 & XB-70

# Conceptual Idea Behind ILAF

The EOM for the  $i$ 'th elastic modal coordinate is

$$\ddot{\eta}_i + 2\zeta_i\omega_i\dot{\eta}_i + \omega_i^2\eta_i = Q_i / \mathcal{M}_i$$

The generalized force from a force  $F$  applied at point  $P$  is

$$Q_i = \phi_i(x_P, y_P, z_P) \cdot F$$

If the force is proportional to the negative local velocity then

$$F = -K \left. \frac{d\mathbf{d}_E}{dt} \right|_{Body} (x_P, y_P, z_P) = -K \sum_{i=1}^n \phi_i(x_P, y_P, z_P) \dot{\eta}_i$$

Hence the generalized force becomes

$$Q_i = -K \phi_i(x_P, y_P, z_P) \cdot \sum_{j=1}^n \phi_j(x_P, y_P, z_P) \dot{\eta}_j = \boxed{-K' \dot{\eta}_i} + \sum_{\substack{j=1 \\ j \neq i}}^n K_j \dot{\eta}_j$$

Where  $K' > 0$

Substitution in to EOM yields increased damping

# ILAF Applied to BFF Vehicle

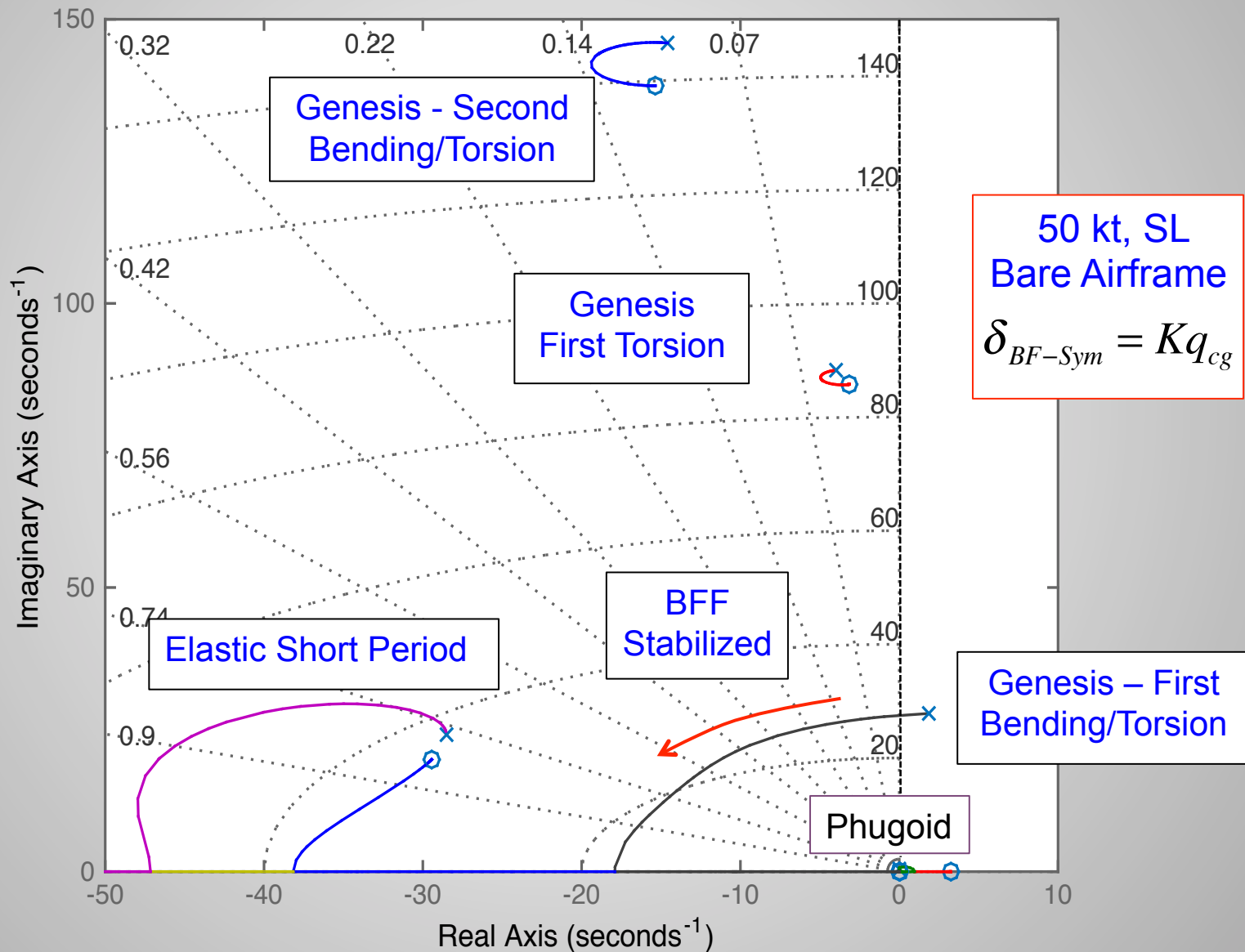
## Sensor-Actuator Selection

- BFF condition - interactions between the vehicle pitch-dominant mode (elastic-short-period) and the first aeroelastic mode
- First aeroelastic mode involves bending, center-body pitching, and wing twist.
- “Rigid-body” pitching replaces wing twist in the conventional bending-torsion flutter mechanism.
- Second flutter mode is more classical bending-torsion – max deflection at wing tips
- Corollaries to ILAF –
  1. Apply pitching moment to location on the structure proportional to pitch rate measured at the same location.
  2. Apply wing torque at tips proportional to wing-tip twist.
- Approximate ILAF – feedback center-body pitch rate to body flaps and feedback wing-tip twist to outboard flaps

# Gain Root Locus - BFF Stabilized

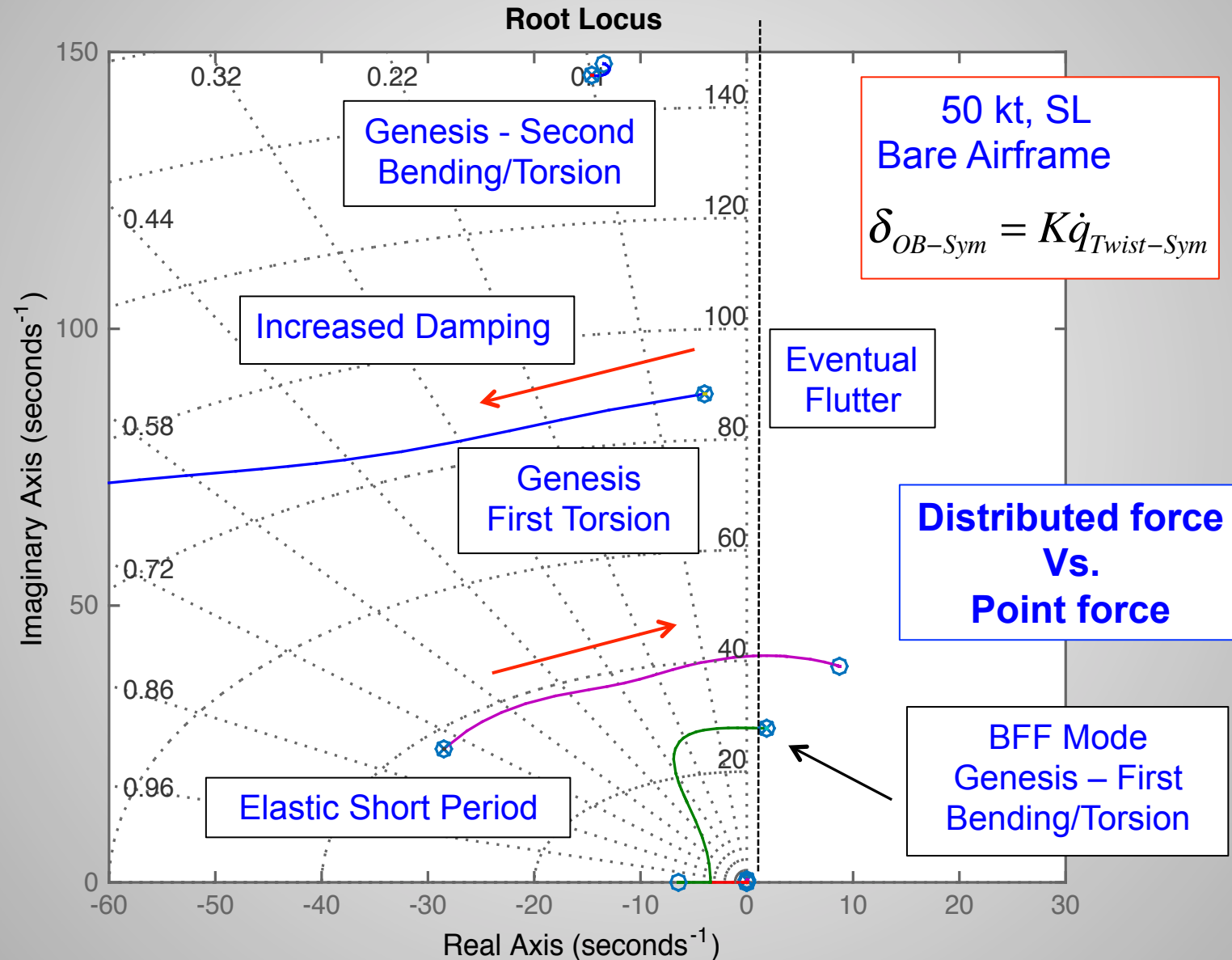
## Pitch Rate to Body Flap

Root Locus



# Second Flutter-Mode Suppression

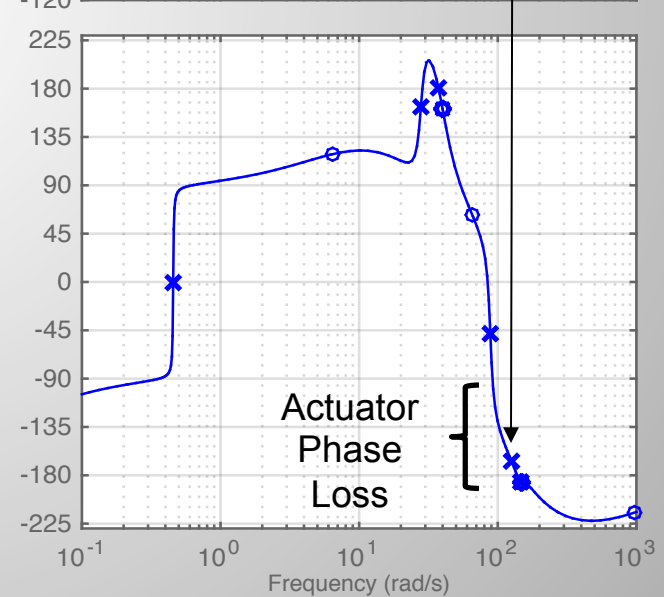
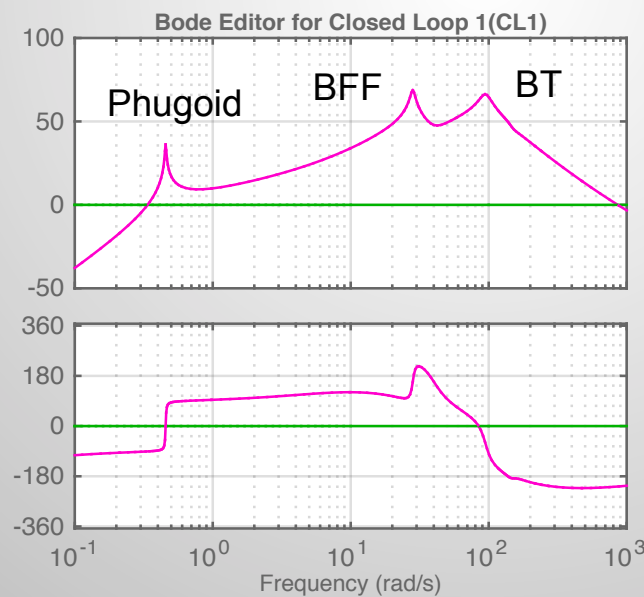
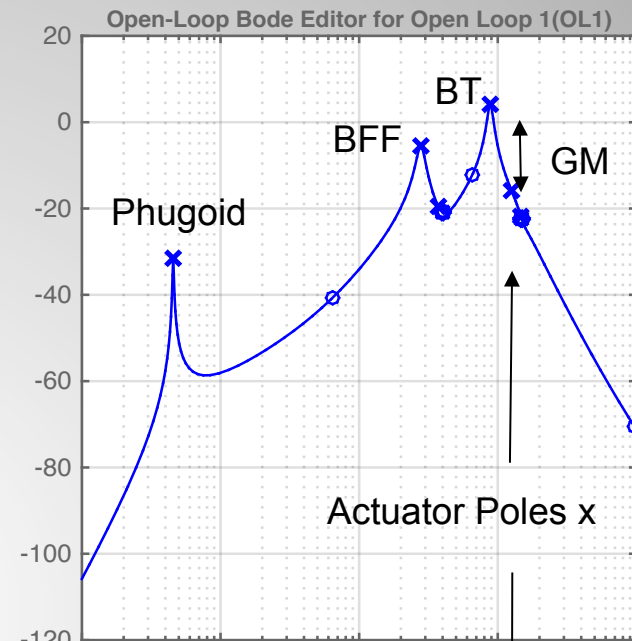
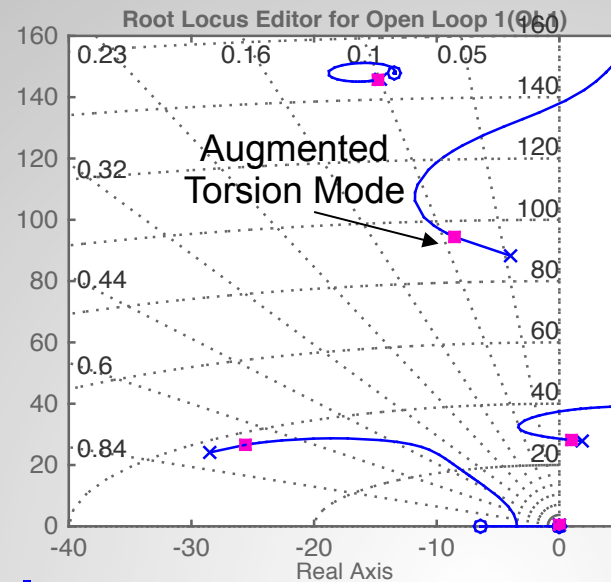
## Wing-Tip Twist Accel. to Outboard Flaps





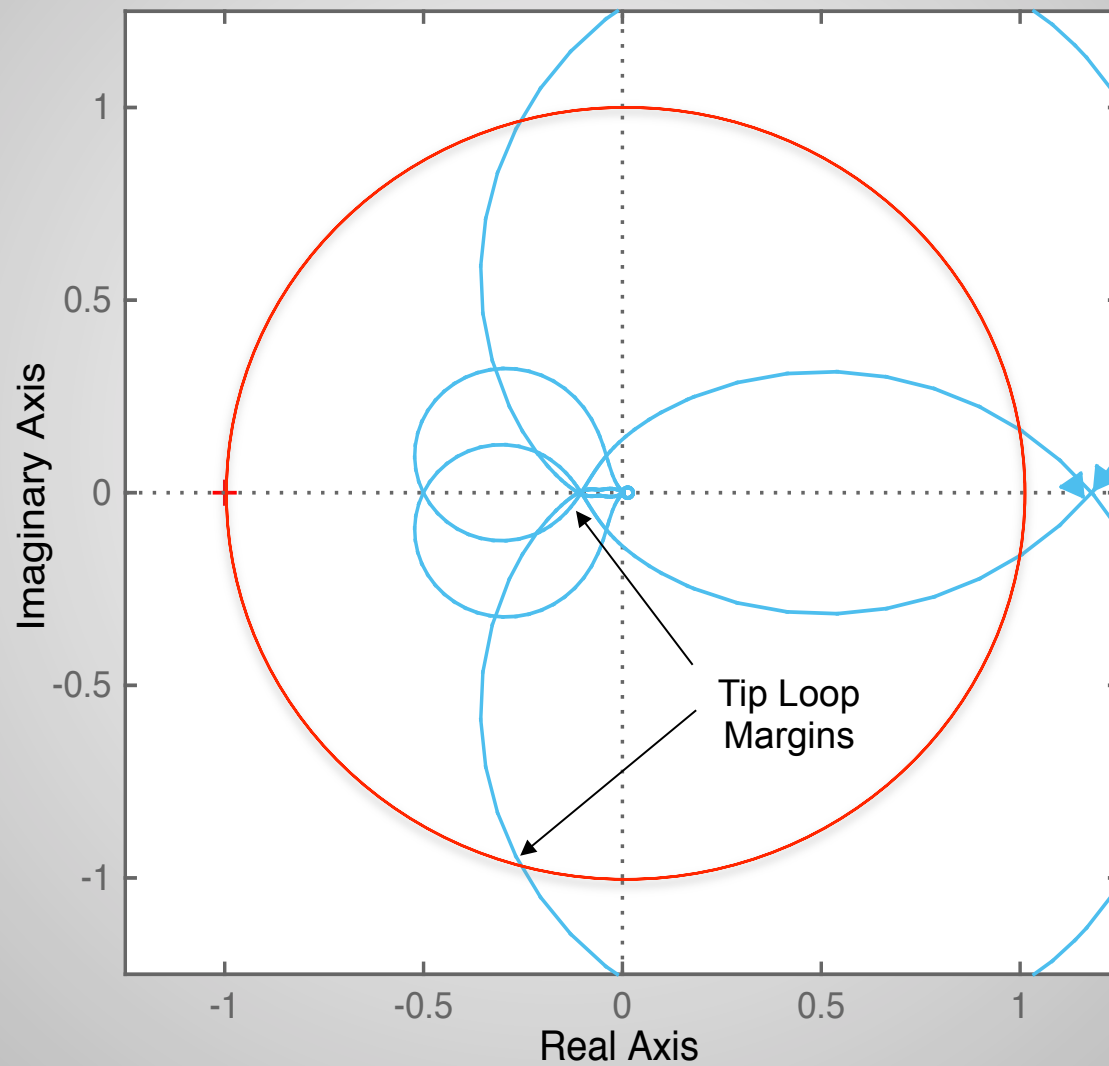
# With Actuators – 50 kts

## MATLAB's Control Design Tool



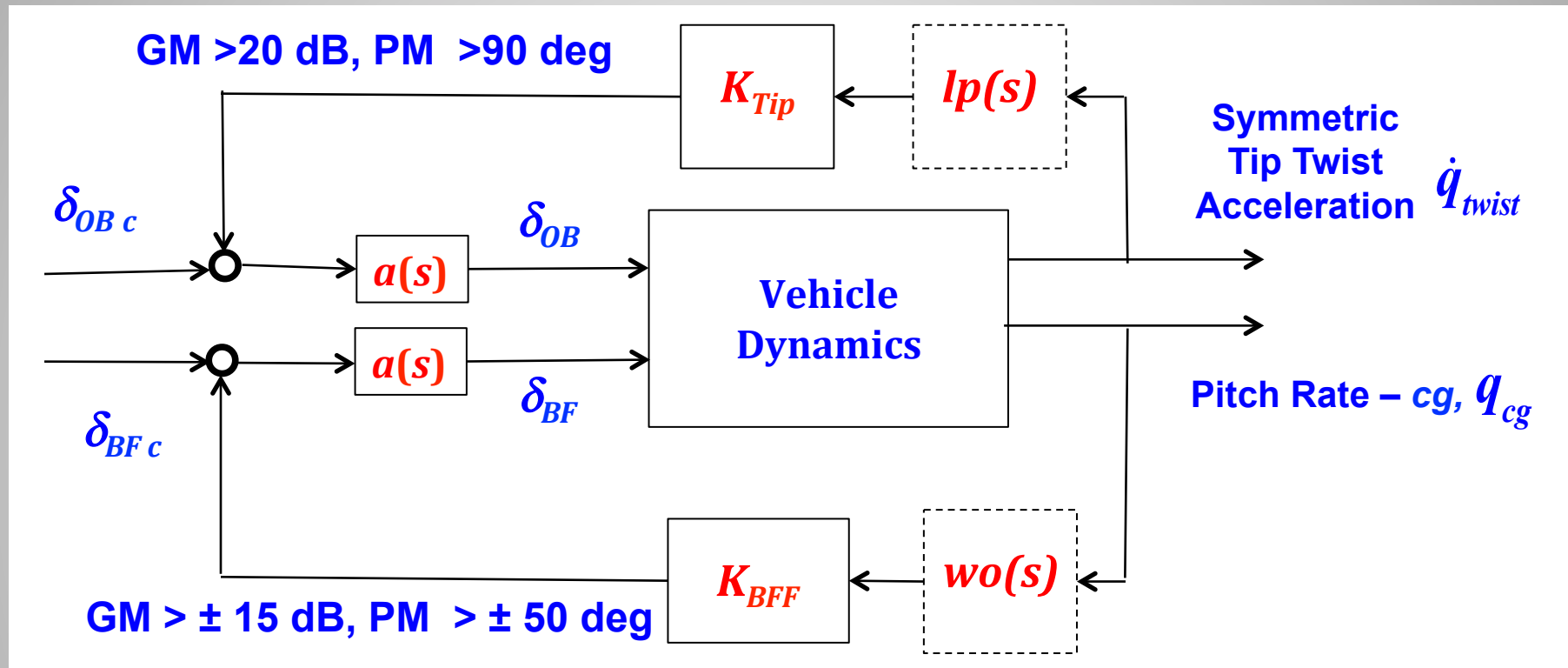
# Tip-Twist Loop Nyquist

Nyquist Diagram



# Control-Law Architecture – ILAF

V = 50 and 60 kts



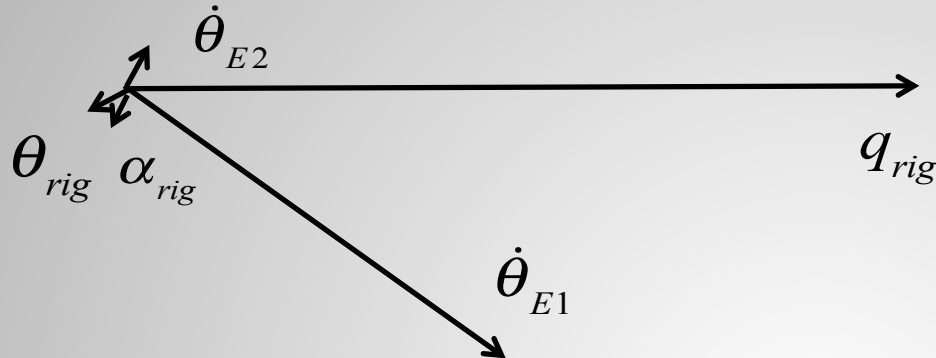
Center-body pitch rate to symmetric body flap –  $K_{BFF} \sim 0.2 \text{ deg/deg/sec}$

Symmetric blended accelerometer to symmetric outboard flap  
 -  $K_{Tip} \sim 0.0005 \text{ deg/deg/sec}^2$

Notes: Second flutter mode (torsion) suppression is actuator limited at 60 kt  
 Washout and low-pass filters also being considered

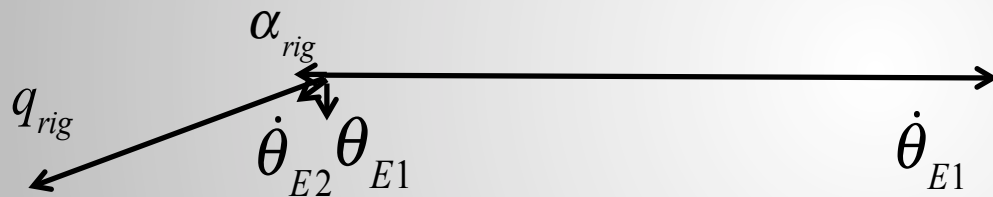
# The Mode Shapes – 50 kts

## Unstable



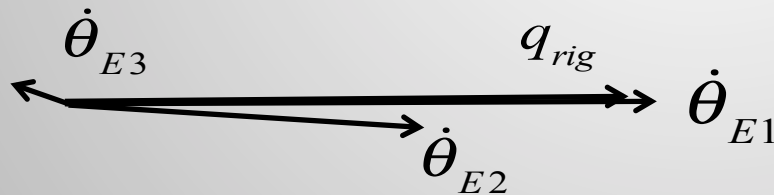
Elastic Short Period

$$\lambda = -28.5 \pm 24.1j$$



1<sup>st</sup> Aeroelastic - BFF

$$\lambda = 1.9 \pm 27.8j$$

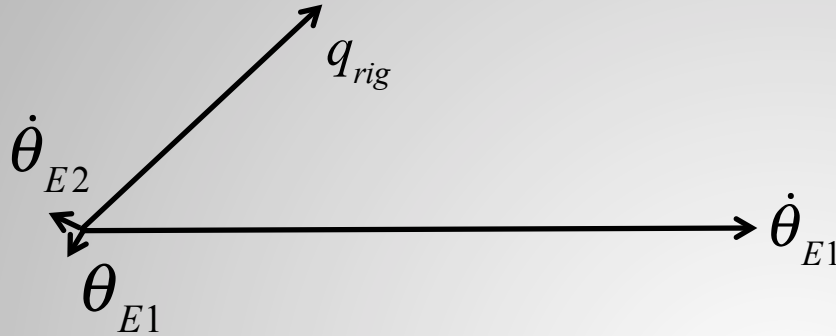


2<sup>nd</sup> Aeroelastic – Torsion

$$\lambda = -4.0 \pm 88.3j$$

# Mode Shapes – 50 kts

## Augmented



Former Elastic Short

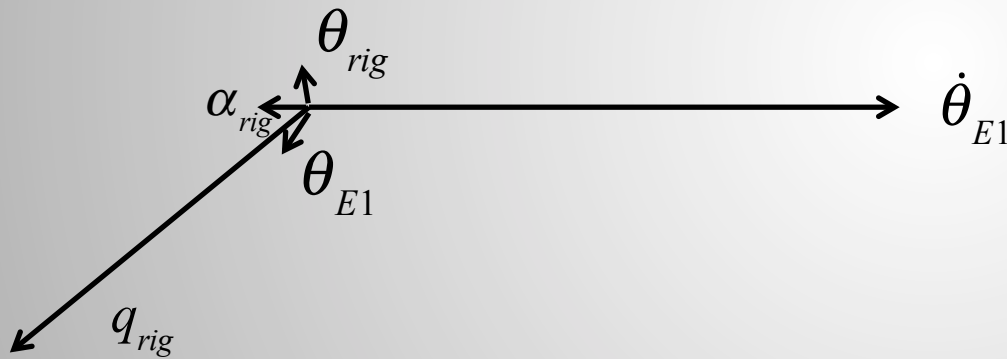
Period

$$\lambda = -33.6 \pm 35.7$$

Stabilized BFF

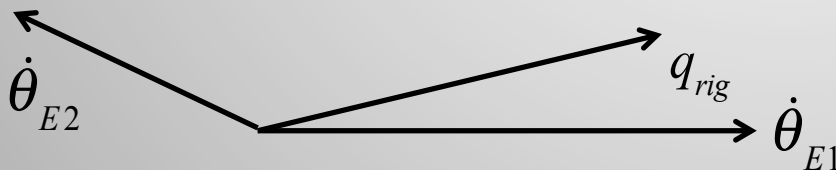
New Elastic Short Period

$$\lambda = -12.1 \pm 16.1j$$



2<sup>nd</sup> Aeroelastic (Torsion)

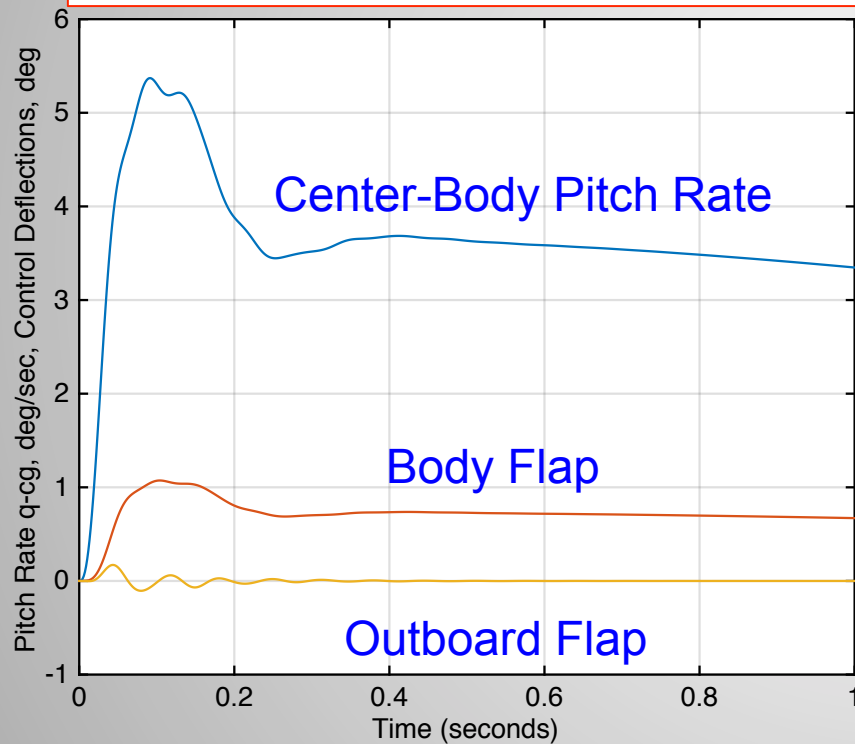
$$\lambda = -17.3 \pm 83.1j$$



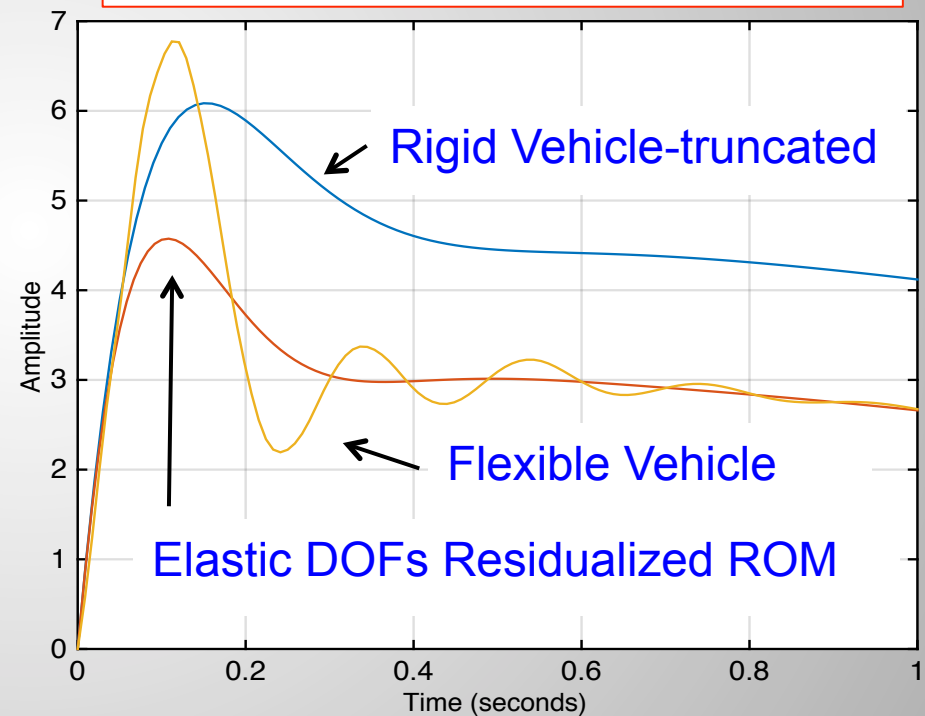
# Closed-Loop Pitch-Rate Step Responses

$$\delta_E = -1 \text{ deg}$$

Center-Body Pitch-Rate (deg/sec)  
 $50 \text{ kt} > V_{\text{BFF}}$



Center-Body Pitch-Rate (deg/sec)  
 $35 \text{ kt} < V_{\text{BFF}}$



**Based on These Results,  
Addition Pitch Stability Augmentation  
May Not Be Required**

# Summary and Conclusions

- Longitudinal nDOF “Flight-Dynamics” model developed
- Good agreement with LM flutter predictions and flight test results
- Vehicle exhibits highly coupled “RB” pitch and 1<sup>st</sup> aeroelastic modes
- AFS stabilized both BFF and BT flutter modes, at both 50 and 60 kt.
- Reasonable margins achieved in all cases ( $> \pm 12$  dB,  $> \pm 40$  deg)  
Including effects of actuator bandwidth (125 rad/sec).
- Simple, two-loop, constant-gain architecture with sensor blending.
- Reasonable pitch responses – similar to that for stable vehicle  $< V_{BFF}$
- Modest control-surface demands

1. Schmidt, MATLAB-Based Flight-Dynamics and Flutter Modeling of a Flexible Flying-Wing Research Drone,” DKS PAAW Working Paper, January, 2015. Submitted to *Journal of Aircraft*.
2. Schmidt, “Integrated Stability Augmentation and Active Body-Freedom-Flutter Suppression For a Flexible Flying-Wing Research Drone,” DKS PAAW Working Paper, January, 2015. Submitted to *JGCD*.



**Backups**

# Design-Cycle Time Line (Notional)

Preliminary  
Conceptual  
Design

Final  
Detail  
Design

Manufacturing  
And  
Assembly

Aerodynamic  
Design



Structural  
Design



Structural  
Detail  
Design



FEM  
Vibration  
Model



Flight Control  
and  
Active Structural  
Mode Control  
Design



**Crunch Time**

# **Simplifications Employed to Obtain “Early” Model**

- **Use rigid-body aero data and model the rigid vehicle first**
- **Start with quasi-steady aero in aeroelastic analysis**
- **Use simple beam-element FEM for vibration analysis**

# Data Sources for This Task

**FEM - UMN**

**Mass properties - UMN**

**Aerodynamics**

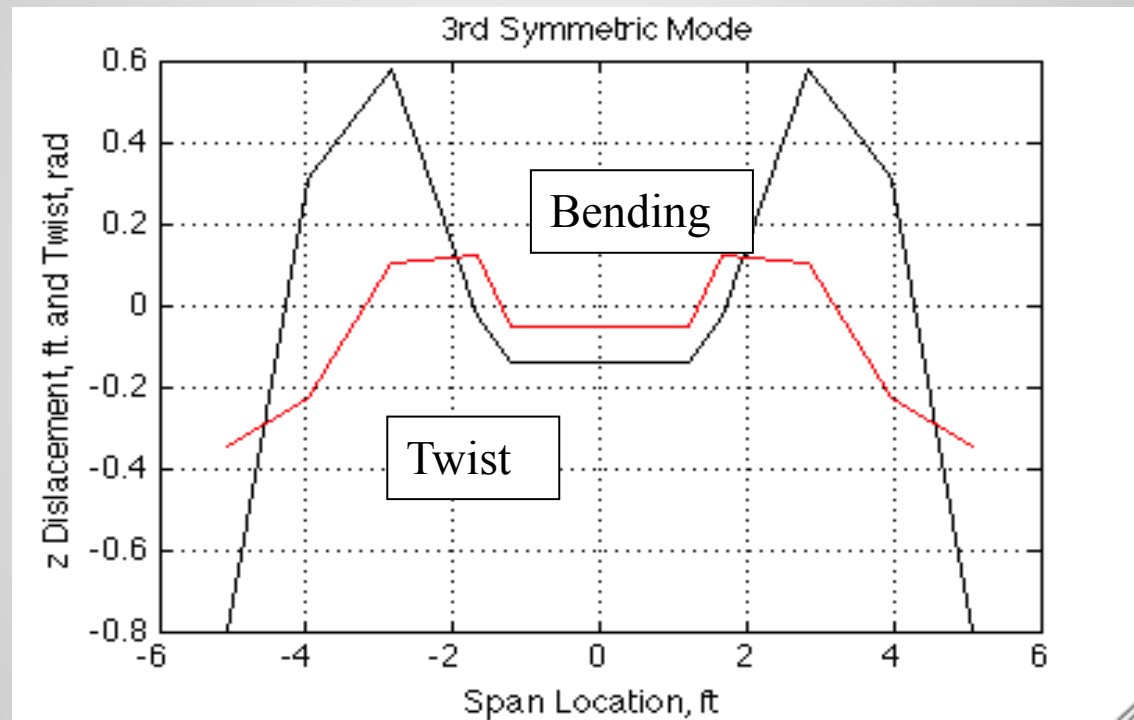
**Digital DATCOM (slender-wing, empirical)**

**Strip theory**

**VLM**

**DLM later**

# Third Symmetric Mode



# Aero Stability Derivatives

**Table 3, Rigid-Body Longitudinal Stability Derivatives**

$C_{L_\alpha}$ /rad	$C_{M_\alpha}$ /rad	$C_{L_q}$ /rad	$C_{M_q}$ /rad	$C_{D_\alpha}$ /rad	$C_{L_{\delta_1}}$ /rad	$C_{M_{\delta_1}}$ /rad
4.074	-0.310	2.657	-3.830	0.129	0.774	-0.014*
$C_{L_{\delta_2}}$ /rad	$C_{M_{\delta_2}}$ /rad	$C_{L_{\delta_3}}$ /rad	$C_{M_{\delta_3}}$ /rad	$C_{L_{\delta_4}}$ /rad	$C_{M_{\delta_4}}$ /rad	
0.630	-0.246	0.530	-0.410	0.301	-0.353	
$C_{D_{\delta_1}}$ /rad	$C_{D_{\delta_2}}$ /rad	$C_{D_{\delta_3}}$ /rad	$C_{D_{\delta_4}}$ /rad			
0.0012	0.0015	0.0018	0.0012			

\* From UMN UAV Lab

$$SM = \frac{-C_{M_\alpha}}{C_{L_\alpha}} = \frac{0.310}{4.074} = 7.6\%$$

$$\frac{\theta(s)}{-\delta_E(s)} = \frac{105.04 (s + 0.049)(s + 6.66)}{(s^2 - 0.0125s + 0.2964)(s^2 + 18.05s + 154.4)} \text{ rad/rad}$$

$$\frac{n_{zcg}(s)}{-\delta_E(s)} = \frac{6245 s(s - 0.285)(s + 0.3617)(s + 5.64)}{(s^2 - 0.0125s + 0.2964)(s^2 + 18.05s + 154.4)} \text{ ft/sec}^2/\text{rad}$$